

# Engineering Notes

## Quick Access Recorder Data Analysis Software for Windshear and Turbulence Studies

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### Nomenclature

$A_y$	=	lateral acceleration
$a_0$ – $a_3$	=	calibration coefficients
$m$	=	aircraft mass
$T_{\text{wndw}}$	=	window time interval
$V$	=	inertial speed
$V_a$	=	airspeed
$V_w$	=	wind speed
$x, y, z$	=	position coordinates
$Y$	=	side/lateral force
$\alpha$	=	angle of attack
$\beta$	=	sideslip angle
$\delta_F$	=	flap angle
$\varepsilon^{1/3}$	=	eddy dissipation rate
$\lambda$	=	bias in accelerometer
$\sigma_w$	=	standard deviation in vertical wind
$\tau$	=	time lag
$\chi$	=	track angle
$\omega_1, \omega_2$	=	cutoff frequencies in the calculation of eddy dissipation rate

### Subscripts

fin	=	tail fin
fus	=	fuselage
wndw	=	window

### Superscripts

$b$	=	body
$e$	=	Earth

## I. Introduction

**D**UE to terrain effect and land–sea interaction, landing and departing aircraft at Hong Kong International Airport (HKIA)

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could experience low-level windshear and turbulence (viz., occurring below 1600 ft). On average, 1 in 500 flights at HKIA reports encountering significant windshear (headwind/tailwind change of 15 kt or more) and 1 in 2,000 flights reports significant turbulence (moderate or severe). To capture the wind fluctuations, a suite of ground-based and remote-sensing meteorological instruments is operated by the Hong Kong Observatory (HKO), including conventional anemometers, weather buoys, radar wind profilers, a terminal Doppler weather radar and two light detection and ranging (LIDAR) systems. Based on the data collected by these instruments, a number of windshear detection algorithms have been developed by HKO and put into operational use at HKIA. Turbulence detection algorithms are under development as well.

In the development and verification of the preceding algorithms, pilot reports are normally used as sky truth. However, it is commonly accepted that the pilots' perception of windshear and turbulence is subjective, and there could be discrepancies among the reports themselves. To build up an objective database of windshear and turbulence cases, HKO has taken two steps: 1) to obtain quick access recorder (QAR) data routinely from local airlines, and 2) to arrange a collaborative study with an established aerospace laboratory for developing software to process the QAR data and obtain the required meteorological quantities [e.g., the three wind components, windshear hazard factor, and turbulence intensity metrics, such as turbulent kinetic energy (TKE) and eddy dissipation rate (EDR)]. Similar work was done in this area by Bach and Parks [1] and others (see [2–5]).

## II. Basic Features of the Algorithm WINDSTURB

### A. General

The aircraft types considered so far include A320, A330, B747, and B777. The parameters measured onboard the aircraft vary from type to type. Basically, the QAR data can be grouped into several categories; viz., inertial data [e.g., accelerations, groundspeed (GS)], attitude data (e.g., pitch, roll) and attitude rates (if available), aerodynamic data (e.g., calibrated airspeed, Mach number, etc.), etc. The data sampling rates vary for the different parameters and also depend on aircraft type. It is assumed that proper presampling filters have been applied before recording the data. The basis of all postprocessing and calculations is a fixed sampling rate of 4 Hz. For this purpose, data interpolation or reduction is required for various parameters.

### B. Heart of the Algorithm

Detailed descriptions of the algorithm can be found in [6]. Basically, what is needed to determine the wind vector  $\mathbf{V}_w$  is the inertial speed vector  $\mathbf{V}$  and the aerodynamic speed vector  $\mathbf{V}_a$ . The wind vector is simply obtained from the difference:

$$\mathbf{V}_w = \mathbf{V} - \mathbf{V}_a \quad (1)$$

These vectors relate to one and the same reference frame. The reference frames involved are the Earth-referenced frame ( $x, y, z$ ) = (north, east, and vertical), the runway reference frame (same as Earth frame but with  $x$  along the runway centerline), and the body reference frame (with its origin in the aircraft's center of gravity), the  $x$  axis pointing along the fuselage toward the nose, the  $y$  axis pointing toward the starboard wing tip, and the vertical  $z$  axis following the right-hand rule (i.e., downward). A particular reference frame is indicated by superscripts  $b$  or  $e$  for the body or Earth frame, respectively.

One could obtain the wind from the wind data computed by the flight management system (FMS) (the vertical wind component is

not computed), but this information was not always found reliable or accurate. Therefore, it is computed using Eq. (1). The first term (the inertial velocity vector  $\mathbf{V}$ ) in the Earth reference frame is

$$\mathbf{V}^e = \begin{bmatrix} \text{GS} \cos \chi \\ \text{GS} \sin \chi \\ \dot{z} \end{bmatrix}^e \quad (2)$$

The second term (the aerodynamic velocity vector) is obtained in the body reference frame as follows:

$$\mathbf{V}_a^b = \begin{bmatrix} V_a \cos \alpha \cos \beta \\ V_a \cos \alpha \sin \beta \\ V_a \sin \alpha \end{bmatrix}^b \quad (3)$$

Thus, one needs to know the aerodynamic speed  $V_a$ , the angle of attack (AOA)  $\alpha$ , and the sideslip angle  $\beta$ . The aerodynamic speed is computed using a combination of calibrated airspeed, Mach number and/or true airspeed (if recorded on the QAR), etc. Sections II.D and II.E describe how  $\alpha$  and  $\beta$  are obtained.

In subtracting the velocities in Eq. (1), these are referenced in the same reference frame, using suitable axis transformations.

### C. Kalman Filtering and Smoothing

A main feature of WINDSTURB is the use of Kalman filtering and smoothing. It is a process of estimating the state vector  $\mathbf{x}$  of a dynamical system at a particular stage  $i$  (or time  $t_i$ ) and its covariance, where  $\mathbf{x}$  consists of three inertial velocities, three positions, and three accelerometer biases, using measurements of inertial data (e.g., track, GS), attitudes, barometric and radio altitudes, etc. Furthermore, estimates of the accuracy with which parameters have been measured were derived, sometimes by trial and error. The Kalman filter process is generally well known in literature; however, the smoothing process has not found wide application. Both are described in detail in [7]. The Kalman filter-smoother combination was applied specifically in order to estimate the vertical velocity as accurately as possible.

A typical result is given in Fig. 1, which shows the estimate of the inertial vertical velocity  $\dot{z}$ , as well as its standard deviation  $\sigma_z$  as it developed for a particular landing approach.

The vertical velocity varies from +4 m/s (descent at 790 feet per minute) to near zero at  $t = 250$  s and, finally, back to zero again at the end (landing). The standard deviation of the vertical velocity starts off at about 0.7 m/s, and then it drops quickly to 0.5 m/s, where it more or less stays constant (the steady-state value). At the point where the more accurate radio altitude is used (about 400 s), it drops further to 0.2 m/s. This shows that the overall accuracy in the estimated vertical velocity, and hence the wind component, is in the order of 0.5 m/s (1 kt) or better, but it also shows that it is a dynamic process.

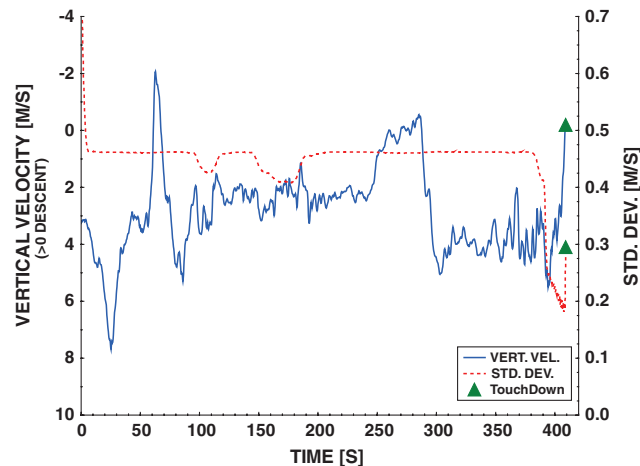


Fig. 1 Envelope of vertical velocity and standard deviation.

### D. Angle-of-Attack Calibration

One aerodynamic parameter needed in Eq. (3) is the AOA  $\alpha$ , to be obtained from the measured AOA vane data. The relationship between these two is the calibration equation. Since these calibration data are usually proprietary, they were derived from the QAR data.

Posing the calibration equation generally as

$$\alpha_i = a_o + a_1 \cdot \text{AOA}_{i+\tau} + a_2 \cdot \delta_{Fi} + a_3 \cdot \text{AOA}_{i+\tau} \cdot \delta_{Fi} \quad (4)$$

the calibration coefficients  $a_0$ – $a_3$  and time delay  $\tau$  are determined once per aircraft type through a multiple regression analysis.

### E. Sideslip Angle Estimation

In all the QAR data considered so far, there is no measurement of the sideslip angle, as it is assumed to be negligible, so an estimation process has been developed [6,8]. Principally,  $\beta$  is derived from the assumption that the lateral force on the aircraft comes from 1) the tail fin due to the sideslip angle and 2) the fuselage contribution due to sideslip. The lateral specific force  $Y/m$  equals the lateral acceleration (minus bias correction), so one can write

$$\frac{Y}{m} \equiv A_y - \lambda_y = \frac{Y_{\text{fin}} + Y_{\text{fus}}}{m} \quad (5)$$

After some manipulation, one can derive (see [8])

$$\beta = -K_\beta m (A_y - \lambda_y) \quad (6)$$

where  $K_\beta$  is a complicated function specific for each aircraft type. A typical time history of the sideslip angle for a B777 landing approach is shown in Fig. 2.

Average sideslip varied between  $\pm 2$ – $3^\circ$ . At the end of the flight, the sideslip peaks to  $+11^\circ$  as the plane is sideslipping to counteract the crosswind. If wind computations had been uncorrected for  $\beta$ , then the computed wind direction would have lined up with the runway track.

All of the preceding computations can be cast into a computational flowchart, found in Fig. 3.

### F. Turbulent Kinetic Energy and Windshear

Finally, the wind components from Eq. (1) are in the  $E$  frame:

$\mathbf{V}_w^e = \mathbf{V}^e - \mathbf{V}_a^e = \mathbf{V}^e - [\mathbf{T}_{be}]^T \mathbf{V}_a^b$ , where  $[\mathbf{T}_{be}]$  is the body–Earth transformation matrix or, in component form,

$$\begin{bmatrix} V_{wx} \\ V_{wy} \\ V_{wz} \end{bmatrix} = \begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{z} \end{bmatrix} - [\mathbf{T}_{be}]^T \begin{bmatrix} V_a \cos \alpha \cos \beta \\ V_a \cos \alpha \sin \beta \\ V_a \sin \alpha \end{bmatrix}$$

With the wind vector known, the windshear parameter hazard  $F$  is calculated from

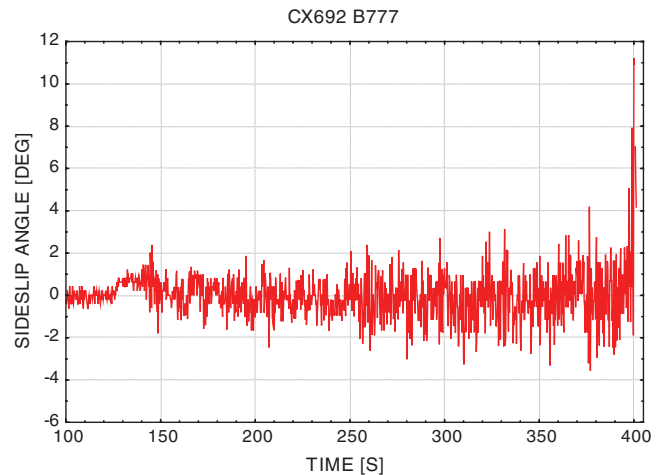


Fig. 2 Sideslip angle during typical flight (B777).

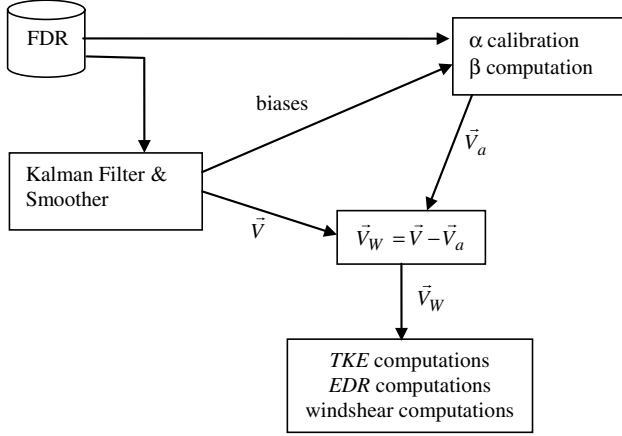


Fig. 3 Flowchart of relevant computations (FDR denotes flight data recorder).

$$F(t) = -\frac{1}{g} \dot{\mathbf{V}}_w(t) \cdot \frac{\mathbf{V}_a(t)}{\|\mathbf{V}_a(t)\|} - \frac{\mathbf{V}_w(t) \cdot \mathbf{k}}{V_a} \quad (7)$$

where  $\mathbf{k}$  is the unit vector along the vertical axis (positive into the earth). The definition is such that, for a downdraft ( $V_{w_z} > 0$ ), the  $F$  factor is negative, as an energy loss is implied.

The TKE is then computed from

$$\text{TKE} = \frac{1}{2}(\sigma_u^2 + \sigma_v^2 + \sigma_w^2) \quad (8)$$

The standard deviations  $\sigma_u$ ,  $\sigma_v$ , and  $\sigma_w$  in the three wind components are computed around a central-moving average wind vector, with a window length of  $T_{\text{wndw}}$ , where  $T_{\text{wndw}}$  is specified by the program user.

### III. Calculation of Eddy Dissipation Rate

The calculation of EDR requires the solution of the power spectrum of the vertical wind component over a selected time window. With the wind-based method preferred (see [9]), a more practical approach is to employ a running mean standard deviation calculation of the bandwidth-filtered vertical wind [10]:

$$\varepsilon^{1/3} = \frac{\hat{\sigma}_w}{\sqrt{1.05 V_a^{2/3} (\omega_1^{-2/3} - \omega_2^{-2/3})}} \quad (9)$$

A sensitivity study of EDR computation with respect to the input parameters (see [10]) showed that there is no need to apply a low-pass filter to the vertical wind signal. Only high-pass filtering is required. The influence of the high-pass frequency on EDR appeared to be rather small. It is suggested to use  $f_1 = 2\pi\omega_1 = 0.1 - 0.2$  Hz and  $f_2 = 2$  Hz in Eq. (9). The moving time window length of 10–20 s also appears to be appropriate.

### IV. Application Examples

The first case is a windshear event, analyzed in [11] (a B747-400 landing at HKIA on 29 March 2005). The pilot reported encountering windshear of +40 kt headwind gain during landing. From the wind speed computed from the QAR data, there is a wind change (increase) of ~12 m/s (24 kt) at about 2 n mile from touchdown (Fig. 4).

This wind change is less than the magnitude of windshear reported by the pilot. To reveal what happened, the airspeed and GS of the aircraft are plotted together in Fig. 5.

At 3 n mile from touchdown, both the airspeed and the GS are almost the same. Then the airspeed increases by about 20 m/s (40 kt). However, the also GS increases but by about 10 m/s (20 kt) only. It turned out that the aircraft was under the control of autopilot C in command mode, but the autothrottles had not been engaged, so the pilot who was flying must have manually controlled the speed with

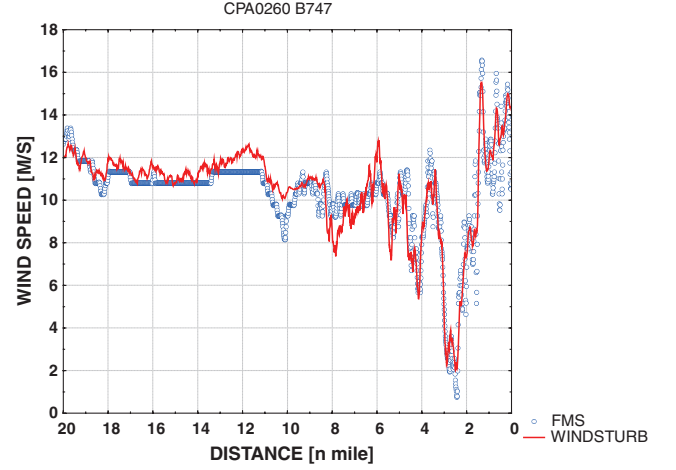


Fig. 4 Wind variation along the approach.

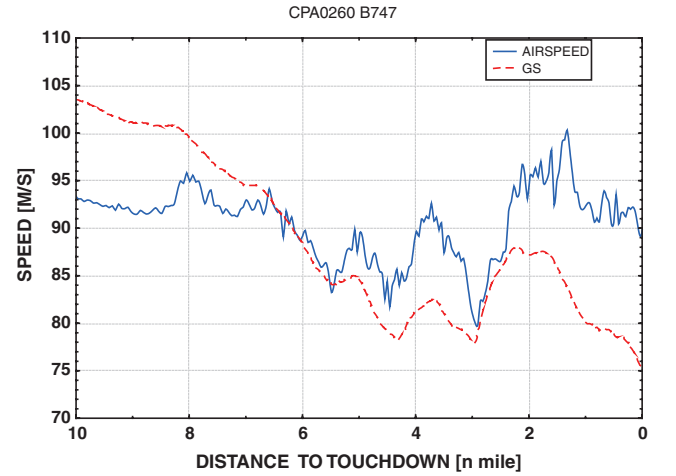


Fig. 5 Airspeed and GS versus distance to touchdown for the B747 flight.

the throttles. Therefore, the pilot-reported wind change of +40 kt was actually an airspeed change of +40 kt due to 1) a windshear of only 20 kt and 2) a GS increase of 20 kt because of pilot action.

A second case concerns the effect of sideslip on the computed TKE and EDR. The change in turbulence, brought about by including the sideslip, is shown in Fig. 6 for a B777 flight.

The TKE with sideslip reached peak values of about  $5.5 \text{ m}^2/\text{s}^2$ , which is 37% higher than the nonbeta peak value of  $4 \text{ m}^2/\text{s}^2$ . The EDR is hardly affected by the sideslip (see Fig. 7), where the peak value of  $0.28 \text{ m}^2/\text{s}^3 \cdot \text{s}^{-1}$  indicates light turbulence [11].

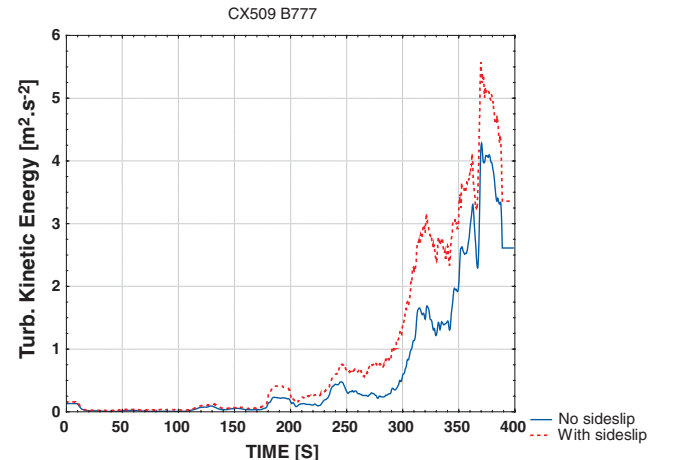


Fig. 6 Effect of sideslip gain on TKE.

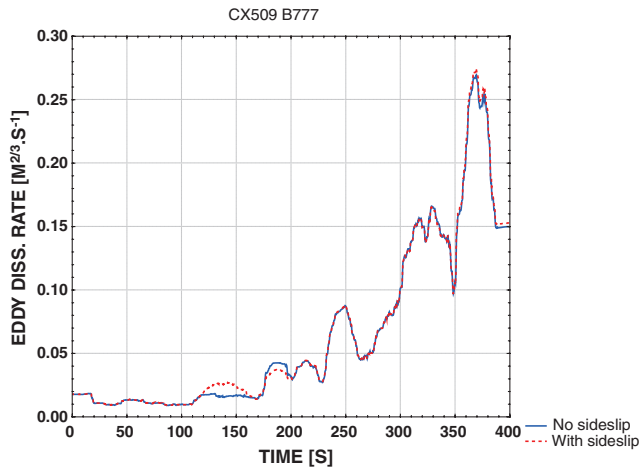


Fig. 7 Effect of sideslip gain on EDR.

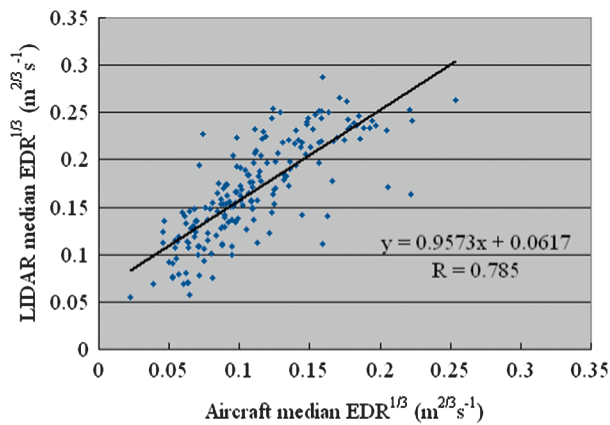


Fig. 8 Comparison of median EDR<sup>1/3</sup> values from the aircraft and from the LIDAR.

Finally, the computed EDR is compared against the LIDAR data measured at the airport [12] (see Fig. 8). Median EDR<sup>1/3</sup> values (between the runway threshold and 4 n mile away) are considered here. The comparison is based on 185 flights in 2006 and 2007. Technical details can be found in [12]. In general, the comparison between the two data sets shows a reasonable correlation.

## V. Conclusions

A sophisticated algorithm has been developed by the National Aerospace Laboratory/NLR and HKO to calculate the meteorological parameters crucial for the study of low-level windshear and turbulence, using onboard QAR data. The resulting calculated windshear and turbulence parameters are found to give valuable insights into the low-level windshear and turbulence events at HKIA. The WINDSTURB program allows batch processing of large

amounts of aircraft QAR data to be completed within several minutes.

The WINDSTURB software will be further refined to cover other aircraft types and expanded to handle missed approaches. The WINDSTURB-calculated  $F$  factor and EDR will also be compared more extensively with the estimates of these quantities from ground-based remote-sensing instruments and pilot reports.

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